# Chapter 6 Notes

**STUDENT COPY**

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<tr>
<th>Marks Requirement</th>
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<tbody>
<tr>
<td>Notes Present</td>
<td>All notes present</td>
<td>Most notes present</td>
<td>Less than half of notes present</td>
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<tr>
<td>Organization / Neatness</td>
<td>Notes in chronological order, name and date on everything</td>
<td>Almost all notes in chronological order, name and date on most pages</td>
<td>Mostly out of order, name and date often missing</td>
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<tr>
<td>Questions</td>
<td>Question column completed on all notes, higher level questions attempted</td>
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<td>Less than half of the question columns complete</td>
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<tr>
<td>Main Ideas and Reflections</td>
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*If your mark does not total up to at least 4 out of 8, your notes are INCOMPLETE and must be fixed up as soon as possible and re-evaluated.*

**TEACHER COPY**

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6.1 – Slope of a Line

Goal: Determine the slope of a line segment and a line.

Toolkit:
- Rate of change
- Simplifying fractions

Main Ideas:

Definitions
Rise: the vertical distance between two points.

Run: the horizontal distance between two points.

Slope: a measure of how one quantity changes with respect to the other, it can be calculated using:

\[
\text{Slope: } \frac{\text{rise}}{\text{run}} = \frac{\text{change in dependent variable}}{\text{change in independent variable}}
\]

Determining the Slope of a Line Segment

Ex 1) Determine the slopes of the following line segments.

Step 1: Choose two points on the line segment.
Step 2: Count the units to determine the rise and the run.
Step 3: Write the fraction in simplest form.

a)

Slope = \frac{\text{rise}}{\text{run}} = \frac{\text{down 3}}{\text{left 2}} = -\frac{3}{2} = -1.5

Line segment EF has slope \(-\frac{3}{2}\).

b)

Slope = \frac{\text{rise}}{\text{run}} = \frac{\text{down 3}}{\text{right 9}} = -\frac{3}{9} = -\frac{1}{3}

Line segment GH has slope \(-\frac{1}{3}\).

When a line segment goes up to the right, both x and y increase. Both the rise and run are positive, so the slope of the line segment is positive.

When a line segment goes down to the right, y decreases and x increases. The rise is negative and the run is positive, so the slope of the line segment is negative.

For a horizontal line segment, the change in y is 0. The rise is 0 and the run is positive.
Slope = \frac{\text{rise}}{\text{run}} = \frac{0}{\text{run}} = 0

For a vertical line segment, y increases and the change in x is 0. The rise is positive and the run is 0.
Slope = \frac{\text{rise}}{\text{run}} = \frac{\text{rise}}{0} = \text{undefined}
Drawing a line segment with a given slope.

Ex 2) Draw a line segment with the given slope.

a) $\text{Slope} = \frac{4}{9}$

b) $\text{Slope} = \frac{-8}{3}$

Finding slope when given two points.

Ex 3) Determine the slope of the line that passes through $E(4, -5)$ and $F(8, 6)$.

Slope of a line $= \frac{y_2 - y_1}{x_2 - x_1}$

$E(4, -5)$ \hspace{1cm} $F(8, 6)$

$\text{Slope} = \frac{-5 - (-5)}{8 - 4} = \frac{6 + 5}{8 - 4} = \frac{11}{4}$

The slope of $EF$ is $\frac{11}{4}$.

How else could we have found the slope?

* Plot the points and graph the line.

* Use the slope given in the problem directly.

* Use the rise over run method.
Ex 4)

Tom has a part-time job. He recorded the hours he worked and his pay for 3 different days. Tom plotted these data on a grid.

a) What is the slope of the line through these points?
b) What does the slope represent?
c) How can the answer to part b be used to determine:
   i) how much Tom earned in $3\frac{1}{2}$ hours?
   ii) the time it took Tom to earn $30$?

\[ \text{Slope} = \frac{\text{rise}}{\text{run}} = \frac{\$24}{2\text{hr}} = 12 \]

The slope of the line is 12.

b) The units are $\$ \text{ per h}$, so the slope represents his rate of pay $= \$12/\text{h}$.

c) We know Tom makes $\$12/\text{h}$ so:
   i) $\$12 \times 3\frac{1}{2} \text{h} = \$42$
   Tom earned $\$42$ in $3\frac{1}{2}$ hr.
   ii) $\$12 \text{ for } 1 \text{ hr}$ so $\$30 = \frac{\$30}{\$12} \times \frac{\text{?}}{1 \text{ hr}}
   \text{?} = 2.5 \text{ or } 2\frac{1}{2} \text{ hr}.

It took Tom $2\frac{1}{2}$ hr to make $\$30$.

Look on the graph to see if your answers to "c" make sense.

Reflection: How is the slope of a line related to rate of change?
6.2 – Slopes of Parallel and Perpendicular Lines

Goal: to use slope to determine whether two lines are parallel or perpendicular.

Toolkit:
- Slope
- Simplifying fractions
- Reciprocals

Main Ideas:

<table>
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<th>Lines that have the same slope</th>
<th>are parallel.</th>
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Ex 1) Line EF passes through E(-4,2) and F(2,-1).
Line CD passes through C(-1,7) and D(7,3).
Line AB passes through A(-4,5) and B(5,1).

Sketch the lines. Are they parallel?

**Recall:** Slope \( \frac{y_2 - y_1}{x_2 - x_1} \)

**Slope EF:** \( \frac{-1 - 2}{2 - (-4)} = \frac{-3}{6} = -\frac{1}{2} \)

**Slope CD:** \( \frac{3 - 7}{7 - (-1)} = \frac{-4}{8} = -\frac{1}{2} \)

**Slope AB:** \( \frac{1 - 5}{-4 - 7} = \frac{-4}{9} \)

EF and CD look like they could be parallel, but calculate the slope to be sure.

EF and CD have the same slope so they are parallel.

The slopes of two perpendicular lines are negative reciprocals; that is a line with a slope \( a \), \( a \neq 0 \), is perpendicular to a line with slope \( -\frac{1}{a} \)

Ex 2) Line ST passes through S(-2,7) and T(2,-5). Line UV passes through U(-2,3) and V(7,6).

Are these lines parallel, perpendicular or neither? Calculate the slopes, and then sketch the lines to verify your answer.

**Slope ST:** \( \frac{-5 - (-7)}{2 - (-2)} = \frac{-12}{4} = -3 \)

**Slope UV:** \( \frac{6 - 3}{7 - (-2)} = \frac{3}{9} = \frac{1}{3} \)

\( -\frac{3}{1} \) and \( \frac{1}{3} \) are negative reciprocals, so ST and UV are perpendicular lines.

Perpendicular = two lines that form a 90° angle.
Ex 3)

a) Determine the slope of a line that is perpendicular to the line through G(-2,3) and H(1,-2).

1st find the slope of GH.

Slope GH = \( \frac{-2-3}{1-(-2)} = \frac{-5}{3} \) → The slope of a line perpendicular (⊥) to \(-\frac{5}{3}\) is the negative reciprocal \(\frac{3}{5}\).

b) Determine the coordinates of J so that line GJ is perpendicular to line GH.

Slope of GJ is \(\frac{3}{5}\) → rise: \(\frac{3}{5}\) → run

Ex 4) EFGH is a parallelogram. Is it a rectangle?

C means that each \(\angle\) is 90°

≠ So lines have be perpendicular to each other which means that the slopes of EH and EF should be negative reciprocals

Slope EH = \(\frac{\text{rise}}{\text{run}} = \frac{-1}{3}\)
Slope EF = \(\frac{\text{rise}}{\text{run}} = \frac{5}{2}\)

These are not negative reciprocals, so the lines are not perpendicular, so not a rectangle

Reflection: What have you learned about parallel and perpendicular lines?
6.4 – Slope-Intercept Form of the Equation for a Linear Function

Goal: to relate the graph of a linear function to its equation in slope-intercept form.

Toolkit:
- Slope of a line \( m = \frac{y_2-y_1}{x_2-x_1} \) \( \rightarrow \) \(\frac{\text{rise}}{\text{run}}\)
- The y-intercept (vertical intercept) of a line is \( b \)

Main Ideas:

The equation of a linear function can be written in the form \( y = mx + b \), where \( m \) is the slope of the line and \( b \) is its y-intercept (with coordinates \((0, b)\)).

\[
y = mx + b
\]

Ex. 1) The graph of a linear function has a slope \( \frac{3}{5} \) and y-intercept of \(-4\).
Write an equation for this function.

\[
y = m x + b
\]
\[
\begin{align*}
&\text{Substitute } m = \frac{3}{5}, b = -4 \\
y = \frac{3}{5}x + (-4)
\end{align*}
\]
\[
y = \frac{3}{5}x - 4
\]

Ex. 2) Graph the linear functions with the following equations:

a) \( y = \frac{1}{2}x + 3 \)

\[
y = mx + b
\]
\[
\begin{align*}
&\text{so: } m = \frac{1}{2} \text{ (slope)} \\
&b = +3 \text{ (y-int)}
\end{align*}
\]

\[
\begin{align*}
\text{step 1: plot } y-\text{int} +3 & \text{ so, plot point } (0,3) \\
\text{step 2: slope of line } = \frac{1}{2} = \frac{\text{rise}}{\text{run}} & \text{ so, from } (0,3) \text{ move "up 1, right 2", then mark a new point}
\end{align*}
\]

\[
\text{step 3: draw line through points w/ruler all the way across graph}
\]

b) \( y = -\frac{3}{4}x - 1 \)

\[
y = mx + b
\]
\[
\begin{align*}
&\text{so: } m = -\frac{3}{4}, b = -1 \\
&\text{step 1: plot } y-\text{int} -1 & \text{ so, plot point } (0,-1) \\
&\text{step 2: slope } = -\frac{3}{4} & \text{ (hint: put neg. on top!)}
\end{align*}
\]
\[
\text{so from } (0,-1), \text{ "run" 3 (drop 3) and "run" 4 (right 4), then mark new point}
\]

\[
\text{step 3: draw line w/ruler through points.}
\]
Ex. 3) Write equations to describe the following functions. Verify the equation.

a) \( y = mx + b \rightarrow \text{need } m \text{ and } b! \)

\[ y = \frac{3}{2}x + 4 \]

\[ b = -3 \quad m = \frac{4}{3} \quad m=2 \]

b) \[ y = 2x - 3 \]

Choosing a point on the line \((-3,-1)\), substitute the coordinates into the equation.

Using an Equation of a Linear Function to Solve a Problem

Ex. 4) The student council sponsored a dance. A ticket cost $5 and the cost for the DJ was $300.

\[ P = \text{Profit} \quad t = \text{tickets} \]

\[ P = 5t - 300 \]

a) Write an equation for the profit, \( P \), on the sale of \( t \) tickets.

\[ P = \text{Income} - \text{Expenses} \]

\[ \text{Income} = 5t \quad \text{Expenses} = 300 \]

\[ P = 5t - 300 \]

b) Suppose 123 people bought tickets. Find the profit.

\[ t = 123 \quad \text{sub } t = 123 \text{ into equation, find } P \]

\[ P = 5(123) - 300 \]

\[ P = 615 - 300 \]

\[ P = 315 \]

\[ \therefore \text{profit was }$315 \]

c) Suppose the profit was $350. How many people bought tickets?

\[ P = 5t - 300 \quad \text{sub. } P = 350, \text{ find } t: \]

\[ 350 = 5t - 300 \quad \text{solve for } t \]

\[ 650 = 5t \quad \frac{650}{5} = t \]

\[ t = 130 \quad \therefore 130 \text{ people bought tickets.} \]

d) Could the profit be exactly $146? Justify the answer.

\[ P = 5t - 300 \quad \text{sub in } P = 146, \text{ find } t \]

\[ 146 = 5t - 300 \]

\[ 446 = 5t \quad \frac{446}{5} = t \]

\[ t = 89.2 \quad \text{but, you must have a WHOLE # of tix, so } P \text{ can't be }$146! \]

Reflection: How do the values of \( m \) and \( b \) in the linear equation \( y = mx + b \) relate to the graph of the corresponding linear function? Use examples to help.
6.5 – Slope-Point Form of the Equation for a Linear Function

**Goal:** to relate the graph of a linear function to its equation in point-slope form

**Toolkit:**
- \( y = mx + b \)
- \( m \) is the slope of the line
- \( b \) is the \( y \)-intercept (vertical intercept) of a line

**Main Ideas:**

What is Slope-Point Form of the Equation of a Linear Function

The equation of a line that passes through \( P(x_1, y_1) \) and has slope \( m \) is:

\[
\begin{align*}
\Delta y &= m \Delta x \\

\begin{array}{c|c|c}
\text{coordinate} & \text{at known point} & \text{coordinate} \\
\hline
\Delta y & \Delta x \\
\hline
\end{array}
\end{align*}
\]

**Notice:** this is just the slope formula rearranged → \( \frac{y-y_1}{x-x_1} = m \) (slope)

\[
\begin{align*}
\frac{y-y_1}{x-x_1} &= m(x-x_1) \\
\Downarrow \quad \text{slope-point form} \\
\Rightarrow y-y_1 &= m(x-x_1)
\end{align*}
\]

**Graphing a Linear Function Given Its Equation in Slope-Point Form**

Ex. 1) a) Identify the slope of the line and the coordinates of a point on the line with this equation:

\[
\begin{align*}
y - 2 &= \frac{1}{3}(x + 4) \\
\text{slope} &= m = \frac{1}{3} \\
\text{coordinates} &= (x_1, y_1)
\end{align*}
\]

*from equation:
\[
\begin{align*}
x_1 &= -4, \\
y_1 &= 2
\end{align*}
\]

b) Graph this equation:

**Step 1:** start with a point on the line, we know \((-4, 2)\) is on the line, so plot \((-4, 2)\).

**Step 2:** use slope of \( \frac{1}{3} \) to find another point.

Start at \((-4, 2)\).

slope = \( \frac{1}{3} \), so up 1, right 3.

place new point, connect w/ruler.
Ex. 2) a) Write an equation in slope-point form for this line:

\[ \text{Need: 1 point on the line, slope of line} \]
\[ \times \text{ point on line is } (-1, -2) \]
\[ \times \text{ slope } (m) = \text{rise} \div \text{run} = \frac{3}{4} \]
\[ \text{sub these into slope-point form} \]
\[ y - y_1 = m(x - x_1) \]
\[ y - (-2) = \frac{3}{4} (x - (-1)) \]
\[ y + 2 = \frac{3}{4} (x + 1) \]

b) Write the equation in part a in slope-intercept form. What is the y-intercept of this line?

\[ y + 2 = \frac{3}{4} (x + 1) \]
\[ y + 2 = \frac{3}{4} x + \frac{3}{4} - 2 \]
\[ y = \frac{3}{4} x + \frac{3}{4} - \frac{8}{4} \]
\[ y = \frac{3}{4} x - \frac{5}{4} \]
\[ y \text{-intercept is } -\frac{5}{4} \]

Ex. 3) a) Write an equation for the line that passes through the points G(-3, -7) and H(1,5) to write an equation in slope-point form, we need:

\[ \text{0 the slope } \text{ and } \text{0 a point. We have a point ... (-3, -7) or (1,5) so... Find slope using slope formula, between the given points.} \]
\[ m = \frac{y_2 - y_1}{x_2 - x_1} \]
\[ m = \frac{-7 - (-7)}{1 - (-3)} \]
\[ m = \frac{0}{4} = 0 \]
\[ m = \frac{5 + 7}{1 + 3} \]
\[ m = \frac{12}{4} = 3 \]

b) Write an equation for the line that passes through the points J(-3, 3) and K(5, -1)

we have a point... either (-3, 3) or (5, -1)

so we just need slope!

\[ m = \frac{y_2 - y_1}{x_2 - x_1} \]
\[ m = \frac{-1 - 3}{5 - (-3)} \]
\[ m = \frac{-4}{8} = \frac{-1}{2} \]

Reflection: Explain how the general expression for the slope of a line can help you remember the equation \[ y - y_1 = m(x - x_1) \]
### General Form of the Equation for a Linear Relation

**Goal:** to relate the graph of a linear function to its equation in general form.

**Toolkit:**
- Slope-Intercept form: \( y = mx + b \)
- Slope-Point form: \( y - y_1 = m(x - x_1) \)
- Rearranging Equations

**Main Ideas:**

**GENERAL FORM** of the Equation of a Linear Relation:

\[
Ax + By + C = 0
\]

where \( A \) is a whole number (not negative), and \( B \) and \( C \) are integers.

**STANDARD FORM** of the Equation of a Linear Relation:

\[
Ax + By = C
\]

---

**What is General Form of the Equation of a Linear Relation?**

**How is Standard Form similar?**

---

**Rewriting an Equation in General Form**

Ex. 1) Write each equation in general form and standard form:

a) \( y = -\frac{2}{3}x + 4 \)

\[
\begin{align*}
(\frac{y}{3}) &= (-\frac{2}{3}x + 4) \\
2x + 3y &= -12
\end{align*}
\]

\[
\text{General Form: } 2x + 3y = -12
\]

\[
\text{Standard Form: } 2x + 3y = 12
\]

b) \( y - 1 = \frac{3}{5}(x + 2) \)

\[
\begin{align*}
(\frac{y}{3}) &= (-\frac{2}{3}x + 4) \\
3y &= -\frac{2}{3}x + 12
\end{align*}
\]

\[
\text{General Form: } 3y = -2x + 12
\]

\[
\text{Standard Form: } 3x + 5y + 11 = 0
\]

---

**Graphing a Line in General Form**

Ex. 2) a) Determine the \( x \)- and \( y \)-intercepts of the line whose equation is \( 3x + 2y - 18 = 0 \):

\[
3x + 2y = 18
\]

\[
\begin{align*}
\text{x-inter: set } y &= 0 \text{ (or cover } y \text{ term), solve for } x. \\
\text{3x} &= 18 \\
x &= 6
\end{align*}
\]

\[
\text{y-inter: set } x &= 0 \text{ (or cover } x \text{ term), solve for } y. \\
2y &= 18 \\
y &= 9
\]

b) Graph the line.

- Plot intercepts
- Connect with ruler

---

**c) Verify that the graph is correct**

Choose pt. on graph \( (2, 6) \):

\[
\begin{align*}
\text{Sub } (2, 6) \text{ into equation } \\
3x + 2y &= 18 \\
3(2) + 2(6) &= 18 \\
6 + 12 &= 18
\end{align*}
\]

\[
\text{LS} = RS, \text{graph is correct}
\]

---

**Graph:**

- Label intercepts
- Connect with ruler
Ex. 3) a) Determine the slope of the line with the equation $3x - 2y - 16 = 0$

First, change to standard form:

\[
3x - 2y = 16
\]

**Method 1**

Turn into slope-intercept form:

\[
3x - 2y = 16
\]

\[
-2y = -3x + 16
\]

\[
y = \frac{3}{2}x - 8
\]

So, the slope is $m = \frac{3}{2}$.

**Method 2**

In General or Standard Form, the slope is $\frac{-A}{B}$ always.

So, put $x$ coeff. on top, $y$ coeff. on bottom, and use opp sign when one between $x$ and $y$ terms.

b) Determine the slope of the line with the equation $5x - 2y + 12 = 0$

First, change to standard form:

\[
5x + 2y = -12
\]

Try shortcut:

\[
slope = \frac{-A}{B} = \frac{-5}{2}
\]

Bottom:

\[
m = \frac{-3}{2}
\]

Check:

\[
5x - 2y = -12
\]

\[
-2y = -5x - 12
\]

\[
y = \frac{5}{2}x + 6
\]

It works!

c) Determine the slope AND the $y$-intercept of the line with the equation $4x - 6y = 0$, then graph the line.

Since we need slope AND $y$-int, just turn into slope-intercept form:

\[
4x - 6y = 0
\]

\[
-6y = -4x
\]

\[
y = \frac{2}{3}x
\]

But, we can write as ...

\[
y = \frac{2}{3}x + 0
\]

\[
slope = \frac{2}{3}
\]

\[
y$-int = 0$
\]

Place point at $y$-int = 0, from there, $m = \frac{2}{3}$, so up 2, right 3.

**Reflection:** Why can't you use intercepts to graph the equation $4x - y = 0$? (where $C = 0$) Connect with ruler.
6.7 – Graphing Linear Functions from all Three Forms

Goal: to recognize the different forms of linear functions, and to graph them using the easiest method.

Toolkit:
- Slope/y-intercept form \( y = mx + b \)
- Point-slope form \( y - y_1 = m(x - x_1) \)
- General \( \rightarrow \) Standard form
  \[ Ax + By + C = 0 \rightarrow A \cdot x + B \cdot y = C \]

Main Ideas:

Ex 1) Label each linear equation as either "mx + b", "pt-slope" or "standard":

- \( y - 4 = 5(x - 3) \) \( \text{pt slope} \)
- \( y = -3x + 5 \) \( \text{slope} \)
- \( 2x + 3y = 9 \) \( \text{standard} \)
- \( y + 1 = \frac{3}{4}(x + 2) \) \( \text{pt slope} \)
- \( 2x - y = -4 \) \( \text{standard} \)
- \( y - \frac{1}{2} = x - 5 \) \( \text{slope} \)
- \( y = \frac{1}{2}x - \frac{3}{4} \) \( \text{slope} \)
- \( y = 0.4x - 0.15 \) \( \text{slope} \)
- \( y = mx + b \) \( \text{standard} \)

Ex 2) Graph the equation \( y = -\frac{3}{2}x + 6 \)

Step 1: decide what form it is in: \( y = mx + b \) state \( m = -\frac{3}{2} \) and \( b = 6 \)

Step 2: for \( y = mx + b \), put a point on the y-axis at "b" (sp. \( 6 \) !)

Step 3: use the slope \( m = -\frac{3}{2} = \frac{\text{rise}}{\text{run}} \) to count up/down 3 and over 2 to a new point

Step 4: connect the dots!

\[ y = mx + b \]
- start at \( b \)
- go up/down and over using slope
- connect the dots!

Hint: if you like \( y = mx + b \), you can change any function to \( y = mx + b \) form and use this method!
Ex 3) Graph the equation \( y + 1 = \frac{3}{4}(x + 2) \)

Step 1: decide what form it is in: point-slope

\[ (x, y) \]

\[ (-2, -1) \]

and slope \( = \frac{3}{4} \)

Step 2: for point-slope, draw in the point \((-2, -1)\)

Step 3: use the slope \( m = \frac{\text{rise}}{\text{run}} = \frac{3}{4} \) to count up/down \( 3 \) and over \( 4 \) to a new point

Step 4: connect the dots!

**point-slope**
- start at the point
- go up/down and over using slope
- connect the dots!

Ex 4) Graph the equation \( 2x + 3y - 6 = 0 \) → \( 2x + 3y = 6 \)

Step 1: decide what form it is in: standard

note: \( \text{slope} = -\frac{2}{3} \)

Step 2: for standard form, find the intercepts (cover x to get y, cover y to get x)

\( x\text{-int} = 3 \quad y\text{-int} = 2 \)

Step 3: plot x- and y-intercepts

\( (3, 0) \quad (0, 2) \)

Step 4: connect the dots! (Can check slope)

**standard form**
- get intercepts
- plot intercepts
- connect the dots!

Reflection: Which form of equation do you prefer to graph? **Up to you!**

Would you change every equation to your preferred form, or use the different methods for the different ones? (You may want to try a few in the homework before you answer!)
6.8 – Equations of Parallel and Perpendicular Lines

Goal: to recognize the different forms of linear functions, and to graph them using the easiest method

Toolkit:
- slopes of parallel lines are equal
- slopes of perpendicular lines are negative reciprocals
  (change sign) (flip)
- to find the equation of a line, you need:
  - slope
  - a point
- passing through → sub in!

Main Ideas:

Ex 1) For a line with the slope $0.7$, what is the slope of a line that is

a) Parallel?
\[ m = 0.7 \]

b) Perpendicular?
\[ \frac{-1}{0.7} = \frac{-10}{7} \]

Ex 2) State the slopes of lines that are:

a) parallel to the line $3x + (2)y - 4 = 0$
\[ m_{\parallel} = \frac{-3}{2} \]

b) perpendicular to $y = \frac{1}{2}x - \frac{3}{4}$
\[ m_{\perp} = -2 \]

Ex 3) For this pair of slopes, what is the value of $k$ if the lines are...

a) Parallel? (equat)
\[ \frac{4}{k}, \frac{2}{1} \]
\[ k = \frac{4 \times 1}{2} \]
\[ k = 2 \]

b) Perpendicular? (neg recip)
\[ \frac{4}{k}, \frac{-1}{2} \]
\[ k = \frac{4 \times 2}{-1} \]
\[ k = -8 \]
Ex 4) Are the pairs of lines parallel, perpendicular, or neither?

Check slopes!

a) \(2x + 3y + 9 = 0\)  
\[y = \frac{2}{3}x + 3\]  
\(m = \frac{-2}{3}\)  
\(m = \frac{3}{2}\)  
\(\Rightarrow\) perpendicular!

b) \(y + 1 = \frac{3}{4}(x + 2)\)  
\(6x - 8y + 3 = 0\)  
\(m = \frac{3}{4}\)  
\(m = \frac{6}{8} = \frac{3}{4}\)  
\(\Rightarrow\) parallel!

Ex 5) Find the equation of the line (in \(y = mx + b\) form) that is parallel to the line \(2x + 3y + 9 = 0\) and has the same \(y\)-intercept as the line \(y = 2x + 4\).

\[\frac{1}{2} \text{ to } 2x + 3y + 9 = 0 \Rightarrow \text{Slope}\]

\(m = \frac{-2}{3}\)  
\(m_{||} = \frac{-2}{3}\)  
\(y\)-int. = same as \(y = 2x + 4\)  
\(b = 4\)

\(y = (\frac{2}{3})x + b\)

\(y = \frac{-2}{3}x + 4\)

Ex 6) Find the equation of the line (in \(Ax + By + C = 0\) form) that is perpendicular to \(y = -3x + 4\) and passes through the point \((6,3)\).

perp. to \(y = -3x + 4\) \(\Rightarrow\) slope is \(-\frac{1}{3}\), our slope is \(\frac{1}{3}\)

passes through \((6,3)\) (sub in)

Choose eq'n (only do one 3)  
\[y = mx + b\]

\(y = \frac{1}{3}x + b\)  
\(y = \frac{1}{3}x + 1\)  
\(3y = x + 3\)  
\(3y = 3x + 3\)  
\(0 = x - 3y + 3\)  
\(-2 = c\)  
\[1x - 3y = -3\]  
\[1x - 3y = -3\]  
\[x - 3y = 0\]

Ex 7) Find the equation of the line that is perpendicular to the \(x\)-axis and passes through the point \((4,3)\).

The \(x\)-axis \(\perp\) vert. lines are perp! Always \(x = \text{number}\)

must be \(x = 4\)

Reflection: What short-cuts have you picked up this unit to make answering the questions faster?

\[Ax + By = C \quad m = \frac{A}{B}\]

\[\text{if they give you y-int., use it! others?}\]